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# Prediction of airfoil performance at high Reynolds numbers

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## Introduction

### Large Scale Wind Turbines

Increasing the rotor size may potentially lead to two obvious aerodynamic issues

- ◆ High Mach numbers in the tip region
  - ◆ Might be harmful for performance
  - ◆ Possible to avoid
- ◆ High Reynolds numbers
  - ◆ Might be beneficial for performance
  - ◆ Hard to avoid



DTU 10 MW Reference Turbine

## Introduction

# Airfoil performance at high Reynolds Numbers

We expect that increasing the Reynolds Number will:

- ◆ Decrease the viscous effects due to the thinning of the boundary layer
- ◆ Promote earlier transition due to increased Reynolds number

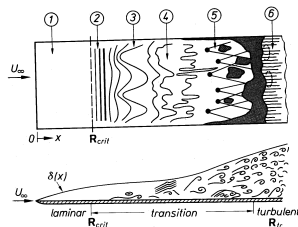
Quantification of the effects can be done by:

- ◆ Measurements
  - ◆ Tunnel measurements are difficult to obtain at high  $Re$  and low Mach
  - ◆ Openly available data are sparse
- ◆ Computations
  - ◆ Model performance in this range is unknown

# Introduction

## Laminar turbulent transition

- ◆ The transition process depend on many parameters
  - ◆ Reynolds Number
  - ◆ Free stream turbulence level
  - ◆ Laminar separation bubbles
  - ◆ Cross flow
  - ◆ Surface roughness
  - ◆ Mass injection
- ◆ Typically approaches for transition modeling
  - ◆  $e^n$  method (Orr-Sommerfeld eqn.)
  - ◆ Empirical correlations
    - ◆ Michel
    - ◆ Mayle
    - ◆ Abu-Ghannam and Shaw
    - ◆ Suzen



## Approach

### The $\gamma - Re_\theta$ Correlation based transition model

- ◆ The model is based on comparing the local Momentum Thickness Reynolds number with a critical value from empirical expressions

$$Re_\theta = Re_{\theta t}$$

- ◆ In the present form the model handles natural transition, by-pass transition, and separation induced transition
- ◆ The model is based on transport equations, and can easily be implemented in general purpose flow solvers

## Approach

 **$E^n$  model for natural transition**

- ◆ The  $E^n$  method is based on analyzing the behavior of small disturbances in the boundary layer

$$\psi(y) = \phi(y) \exp [i(\alpha x - \omega t)]$$

- ◆ The disturbances are inserted in the Navier-Stokes equations, and linearized to give the Orr-Sommerfeld equation

$$(U^* - c^*)(\phi'' - \alpha^2 \phi) - (u^*)'' \phi = \frac{-i}{\alpha Re_\theta} (\phi'''' - 2\alpha^2 \phi'' + \alpha^4 \phi)$$

- ◆ The model is heavily related to BL physics, and not straight forward to implement in general purpose flow solvers.
- ◆ In our inhouse code the EllipSys, the  $E^n$  model can be used together with a bypass and a bubble criteria.

## Approach

### Flow Solver and test cases

- ◆ We use the EllipSys2D incompressible solver.
- ◆ Diffusive terms by second order accurate central differences.
- ◆ Convective terms by QUICK.
- ◆ Steady state computations.
- ◆ Turbulence modeling by the  $k - \omega$  SST model
- ◆ Transitional computations using  $\gamma - Re_{\theta t}$  transition model and  $E^n$  model

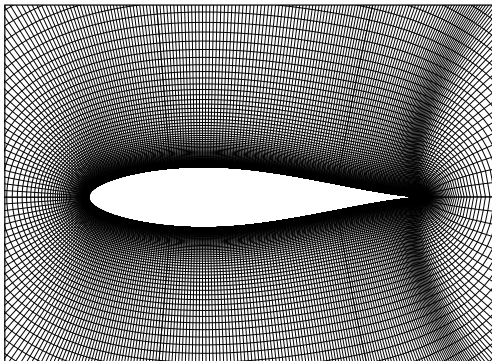
We will analyze a series of airfoils at Reynolds numbers [3-40] million



## Test Case, NACA63-018

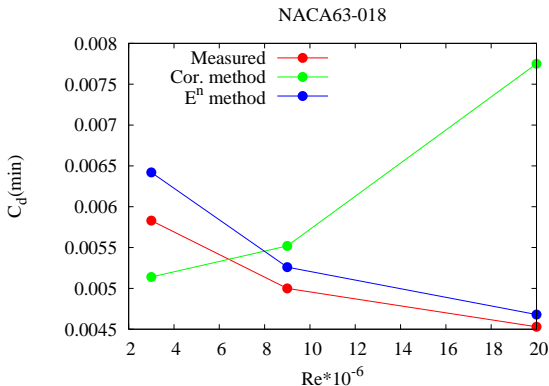
### Computational setup

- ◆ Airfoil computations for  $Re = [3, 9, 20]$  million
- ◆ Using two transition models,  $E^n$  and  $\gamma - Re_\theta$
- ◆ Assuming natural transition ( $N=9$ )
- ◆ Mesh resolution  $384 \times 256$



# Test Case, NACA63-018

## Performance for varying Re

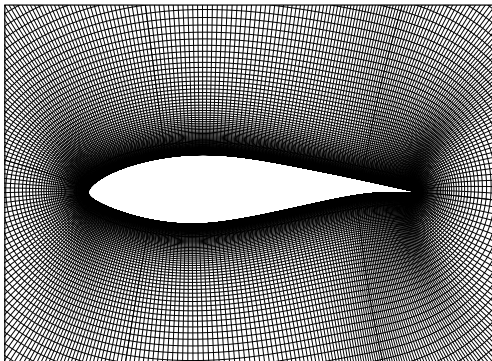


The correlation based model do not respond correctly to varying Re !

## Test Case, DU00-W-212

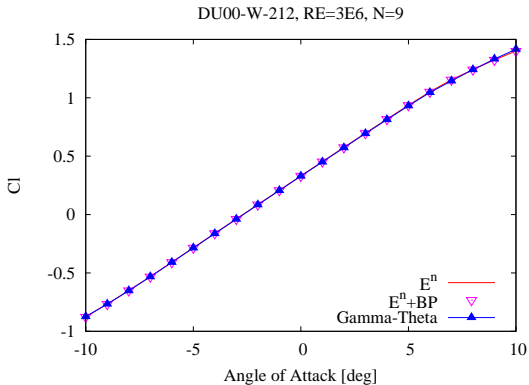
**Computational set-up**

- ◆ Airfoil computations for  $Re=[3, 15]$  million
- ◆ Using three transition models,  $E^n$ ,  $E^n + BP$  and  $\gamma - Re_\theta$
- ◆ All assuming natural transition ( $N=9$ )
- ◆ Mesh resolution  $384 \times 256$



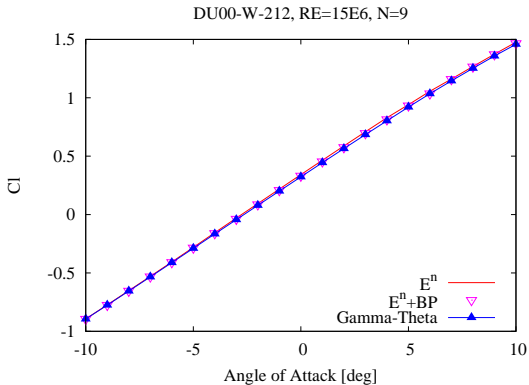
# Test Case, DU00-W-212

## Lift, Natural Transition



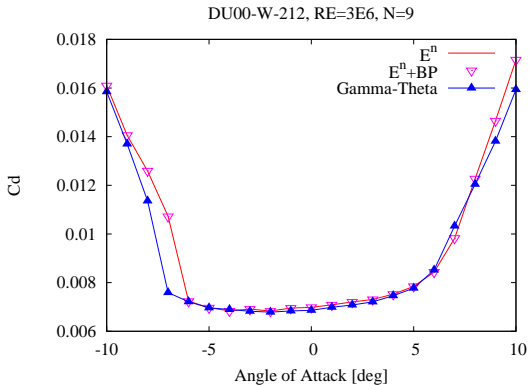
# Test Case, DU00-W-212

## Lift, Natural Transition



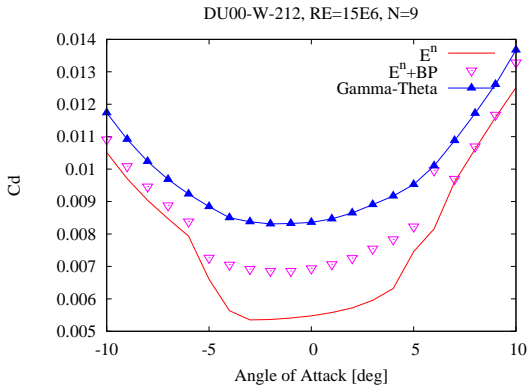
# Test Case, DU00-W-212

## Drag, Natural Transition



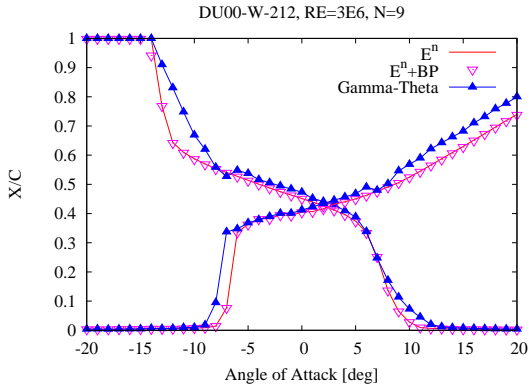
# Test Case, DU00-W-212

## Drag, Natural Transition



## Test Case, DU00-W-212

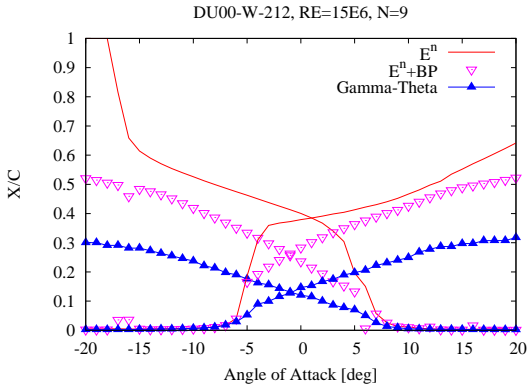
## Transition Location, Natural Transition





# Test Case, DU00-W-212

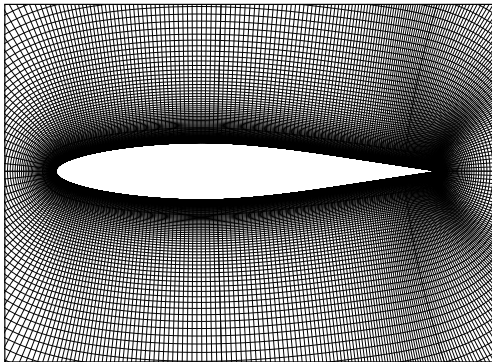
## Transition Location, Natural Transition



## Test Case, NACA64<sub>2</sub>A015

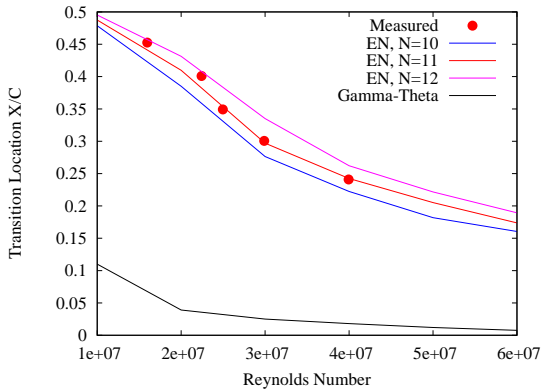
### Computational setup

- ◆ Airfoil computations for  $Re=[10:40]$  million,  $AOA=0$  deg.
- ◆ Using two transition models,  $E^n$  and  $\gamma - Re_\theta$
- ◆ Mesh resolution  $384 \times 256$



# Test Case, NACA64<sub>2</sub>A015

## Performance at high Re

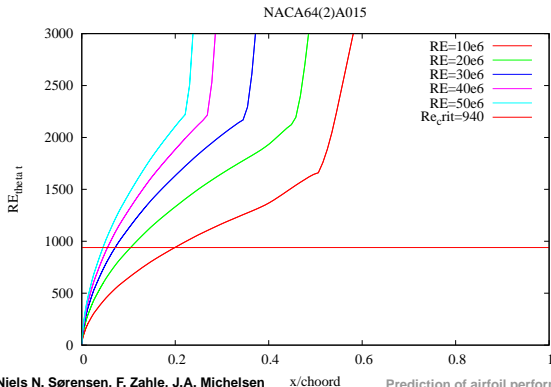


## Explanation

### Behavior of the correlation based model

The following behavior is observed

- ◆ The Reynolds number is varied through the viscosity
- ◆ The pressure distribution stays nearly constant
- ◆ Turbulent quantities are unchanged away from the airfoil
- ◆ The critical Reynolds number predicted by the  $\gamma - Re_\theta$  model stays constant



## Conclusion

### Conclusion and outlook

- ◆ Wind turbine rotors will face high  $Re$  with increasing size
- ◆ Lift is weakly dependent on the transition location in normal operation even at high  $Re$
- ◆ The available data show that the  $\gamma - Re_\theta$  model over-predict drag at high  $Re$
- ◆ The present computations indicate that the  $\gamma - Re_\theta$  model do not react correctly to changes in  $Re$
- ◆ There is very little data available for comparison
- ◆ The present study suggest to use the  $E^n$  model to correctly capture effects of the  $Re$

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